

## Grade 12 (English medium)

### Combined Mathematics – Quadratic Equations

1. If the roots of the quadratic equation  $x^2 + 7x - 5 = 0$ , are  $\alpha$  and  $\beta$  then show that,  $(\alpha^3 + \beta^3) + 7(\alpha^2 + \beta^2) - (\alpha + \beta) = 0$
2. Show that  $ax^2 + bx + c > 0$  when  $a > 0$  and  $b^2 - 4ac > 0$
3. If the roots of the quadratic equation  $ax^2 - bx + c = 0$ , are  $\sin\theta$  and  $\cos\theta$  then show that,  $a^2 + 2ac - b^2 = 0$
4. If the roots of the quadratic equation  $x^2 + x - 1 = 0$ ,  $\alpha$  and  $\beta$  then show that,  $\alpha^2 = \beta + 2$  and  $\beta^2 = \alpha + 2$
5. If the roots of quadratic equation  $\lambda x^2 + \mu(2x + 1) = 0$  has imaginary roots then show that  $\mu x^2 + (\mu - \beta)x = \beta + \lambda - \mu$ . Here  $\beta$ ,  $\lambda$  and  $\mu$  are real constant.
6. The roots of the quadratic equation  $4x(x + 1) - 35 = 0$ , are  $\alpha$  and  $\beta$ . If the roots of the quadratic equation  $\lambda x(x + \mu) - 27 = 0$  are  $2\alpha + \beta$  and  $2\beta + \alpha$  find the value of  $\lambda$  and  $\mu$ .
7. The roots of the quadratic equation  $px^2 + qx + r = 0$ , are  $\alpha$  and  $\beta$ . Then find the quadratic equation which the roots are  $\alpha + \frac{1}{\alpha}$  and  $\beta + \frac{1}{\beta}$ . Here  $p \neq 0$  and  $q \neq 0$
8. Find the necessary condition of one root equal to the  $n$  times of the other root of the quadratic equation  $ax^2 + bx + c = 0$
9.  $\alpha$  and  $\beta$  are the roots of the quadratic equation  $ax^2 + 2bx + c = 0$  and  $\gamma$  and  $\delta$  are the roots of the quadratic equation  $px^2 + 2qx + r = 0$ . If  $\alpha$ ,  $\beta$ ,  $\gamma$  and  $\delta$  are terms of an arithmetic series then show that  $p^2(b^2 - ac) = a^2(q^2 - pr)$ .

10.  $F(x) = (n + 1)x + (n - 1)$ . Here  $x$  is a real number and  $x \neq 0$ .  $n$  is a integer which is greater than 1. Show that  $F(x)$  is not between  $-2\sqrt{n^2 - 1}$  and  $2\sqrt{n^2 - 1}$ . If  $k > 2\sqrt{n^2 - 1}$  then show that the two roots of the quadratic equation  $F(x) = k$

11.  $a$  and  $b$  are two real constant. Show that the roots of the quadratic equation  $a^2(x^2 + 5bx + 4b^2) = 1$  are real and distinct. If  $a > 0$  and  $\alpha, \beta$  are the roots of the above equation and  $\alpha + \beta = 5$  and  $\alpha^2 + \beta^2 = 23$ . Then find the value of  $a, b$  and  $\alpha, \beta$ .

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